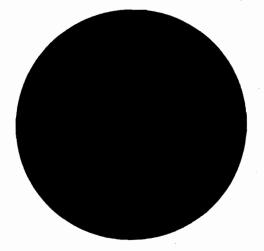
## **Circle Pattern**

T1

Here is a developing circle pattern.

Here is one black circle.



Two white circles of half the radius have been added to the diagram.

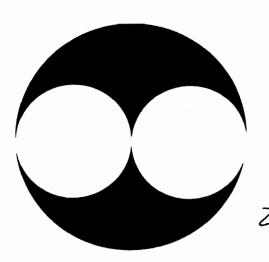
1. Show that the fraction of the diagram that is now black is one half.

rofwhite circle; rof black circle 2r

area black circle TV(2r)?: area white = 2ar²

black circle: 4ra, white circles: 2r²a

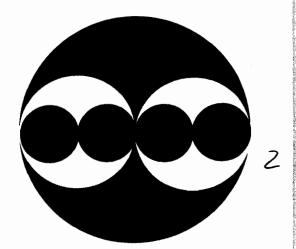
black white = 2r²a, exactly 1/2 of 4TIr²

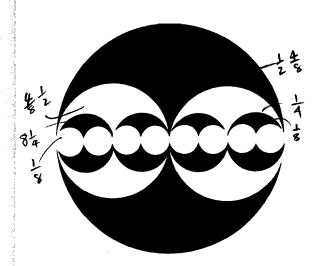


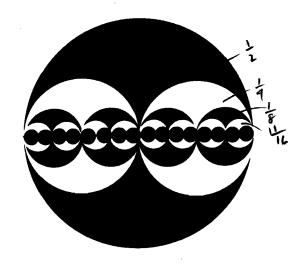
Four black circles have now been added.

2. What fraction of the diagram is now black?

3 ~







| Pattern               | Black fraction | White fraction |
|-----------------------|----------------|----------------|
| One black circle      | 1              | 0              |
| Two white circles     | $\frac{1}{2}$  | $\frac{1}{2}$  |
| Four black circles    | $\frac{3}{4}$  | 4 1 + 1        |
| Eight white circles   | 5 + 1          | 38 -16         |
| Sixteen black circles | 11/4/          | 16             |

4. Write a description of what is happening to the black and white fractions as the pattern continues.

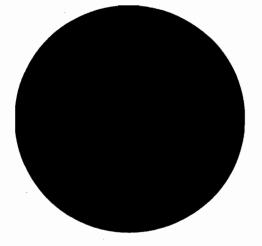
The fractions alternate between adding and subtracting z(denominator) to the pievious fraction, the denominator corresponds whom many of the smallest circles  $E \times 1$ . There smallest ones are 4 black circles, previously  $E \times 1$  of the patter was black, since the smallest circles are the same colour it will increase so  $E \times 1$  to  $E \times 1$  if the color was different, then wo'd subtract.

## **Circle Pattern**

**T2** 

Here is a developing circle pattern.

Here is one black circle.



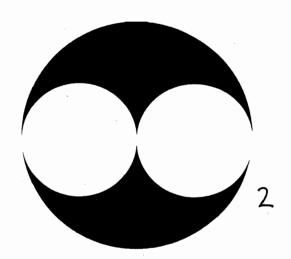
Two white circles of half the radius have been added to the diagram.

1. Show that the fraction of the diagram that is now black is one half.

black circle 
$$\Pi^2$$

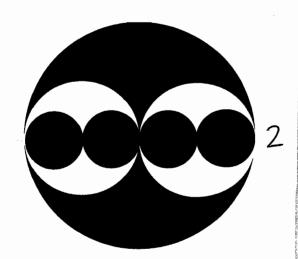
one white circle:  $\Pi(\frac{1}{2}r)^2$ 

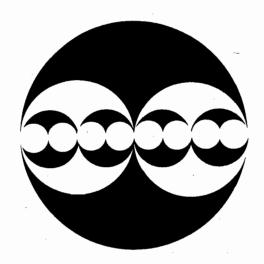
white circles:  $\Pi^{\frac{1}{2}r^2}$ 
 $\Pi^{\frac{1}{2}r^2}$  is  $\frac{1}{2}$  of  $\Pi^2$  so black is the other half of the figure.

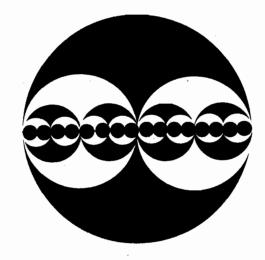


Four black circles have now been added.

One white circle: 
$$\Pi_{4}^{2}$$
 two small black circles:  $\Pi_{4}^{2}$   $\Pi_{5}^{2}$   $\Pi_{5}^{2}$ 







| Pattern               | Black fraction | White fraction |
|-----------------------|----------------|----------------|
| One black circle      | T T            | 0              |
| Two white circles     | 1/2:           | 1<br>2         |
| Four black circles    | 3/4            | 4              |
| Eight white circles   | 5/             | $\frac{3}{8}$  |
| Sixteen black circles | 16/            | 5/16           |

4

4. Write a description of what is happening to the black and white fractions as the pattern continues.

Whenever black circles are added, the black fraction

Increases by half of what was already there, and

the white fraction decreases by half of what was

already there. When white circles are added, the black

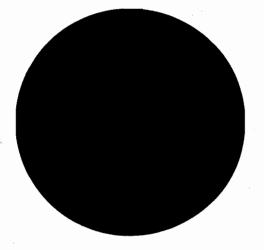
fraction decreases by half of what was already there, and the

Copyright © 2011 by Mathematics Assessment white fraction increases by half of what was

There.

Here is a developing circle pattern.

Here is one black circle.



Two white circles of half the radius have been added to the diagram.

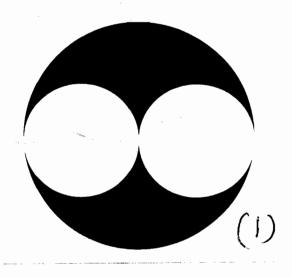
1. Show that the fraction of the diagram that is now black is one half.

If radius of large 
$$C'(rele: 2 \text{ Small:})$$

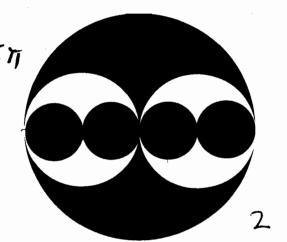
$$(2\times2) \pi = 2(1^2\pi)$$

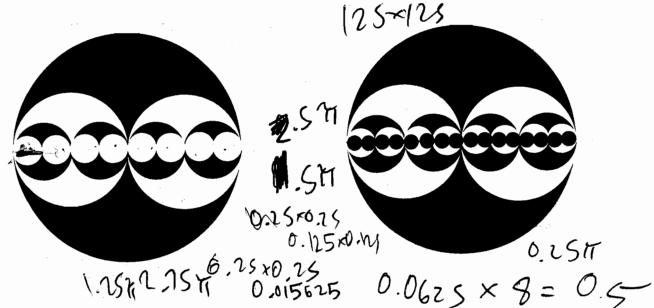
$$4\pi = 2(2\pi)$$

$$4\pi = 4\pi$$



Four black circles have now been added.





| Pattern               |       |       | Black fraction | White fraction |
|-----------------------|-------|-------|----------------|----------------|
| One black circle      | 47    | 271   | 1              | 0              |
| Two white circles     | 21    | W     | $\frac{1}{2}$  | 1/2            |
| Four black circles    | K     | 0.571 | 3/4            | 1/4            |
| Eight white circles   | 6.571 | 6,757 | 5/8/           | 3/9/           |
| Sixteen black circles | 0.250 |       |                | 5/16           |

4. Write a description of what is happening to the black and white fractions as the pattern continues.

The denominators multiply by 2 each

time while when you put in x# 2

of circles you get 1/2x of the original

Circles. Every fine black circles are added

tx black fraction is increased, while \( \frac{1}{2} \times \) is deleted after

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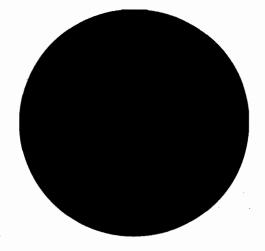
adding white circles. Same for white circles.

## **Circle Pattern**

**T4** 

Here is a developing circle pattern.

Here is one black circle.



Two white circles of half the radius have been added to the diagram.

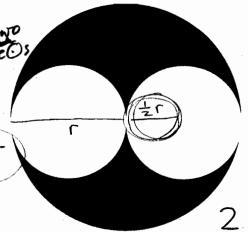
1. Show that the fraction of the diagram that is now black is one half.

area of one black area of the diagram that is now black area of the diagram that is now black is one half.

Лr2 Л2d2, 2 (Лr2), 2Лr2, 4 (Л

27/2 # ## 47/2-2/Tr2=

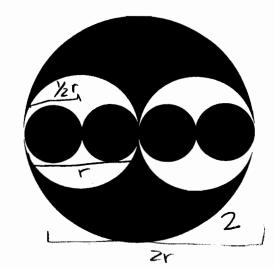
2) Tr2 = 1 black cir-

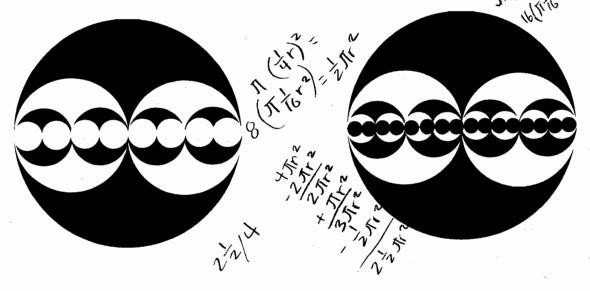


Four black circles have now been added.

BigblackO= 4 
$$\pi r^{2}$$
 white  $0s = 2\pi r^{2}$   
4 Small black=  $(\frac{1}{2}r)^{2}\pi = (4r^{2}\pi)^{4} + 7r^{2}$   
 $4\pi r^{2} - 2\pi r^{2} + \pi r^{2} = 2\pi r^{2} + \pi r^{2} + \pi r^{2} = 2\pi r^{2} + \pi r^{2} + \pi r^{2} = 2\pi r^{2} + \pi r^{2} + \pi r^{2} + \pi r^{2} = 2\pi r^{2} + \pi r^$ 

$$3\pi r^2 = \frac{3}{4}$$
 of diagram





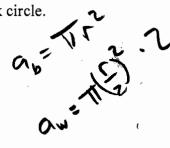
| Pattern               | Black fraction | White fraction |  |
|-----------------------|----------------|----------------|--|
| One black circle      | . 1            | 0              |  |
| Two white circles     | 1/2            | 1 2            |  |
| Four black circles    | 3/4            | 4              |  |
| Eight white circles   | \$ 2/2 /       | 38             |  |
| Sixteen black circles | 11/16          | 5/16/          |  |

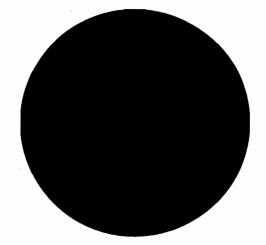
4. Write a description of what is happening to the black and white fractions as the pattern continues.

The white fraction = 1 black circle's fraction. The black circle fraction next in the pattern = the previous white circle (1) fraction + 2. EX.

Here is a developing circle pattern.

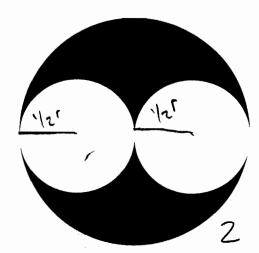
Here is one black circle.



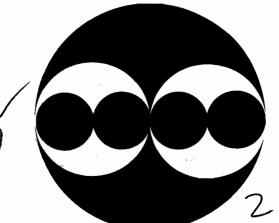


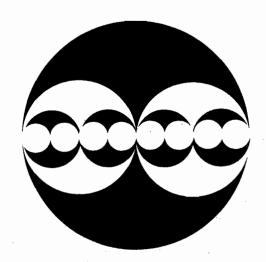
Two white circles of half the radius have been added to the diagram.

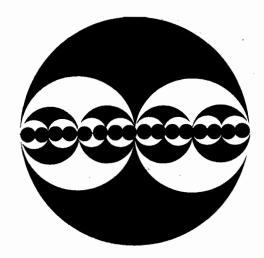
1. Show that the fraction of the diagram that is now black is one half.



Four black circles have now been added.







| Pattern               | Black fraction | White fraction |
|-----------------------|----------------|----------------|
| One black circle      | 1              | 0              |
| Two white circles     | 1/2            | $\frac{1}{2}$  |
| Four black circles    | 3/4 /          | 4              |
| Eight white circles   | 58/            | 3/8            |
| Sixteen black circles | 16/            | 5/6/           |

4

4. Write a description of what is happening to the black and white fractions as the pattern continues.

The pattern is old. Subtract, add, subtract etc.

The number you add/subtract gets smaller by 1/2 reach time. ex. - 1/2, + 1/4, - 1/8, + 1/16. 2