

## Glasses

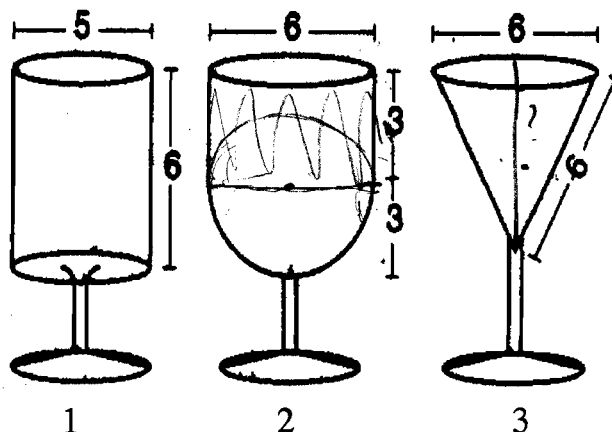
This diagram shows three glasses (not drawn to scale).

The measurements are all in centimeters.

$$\text{The volume of a cylinder} = \pi r^2 h$$

$$\text{The volume of a sphere} = \frac{4\pi r^3}{3}$$

$$\text{The volume of a cone} = \frac{\pi r^2 h}{3}$$



The bowl of glass 1 is cylindrical. The diameter is 5 cm and the height is 6 cm.

The bowl of glass 2 is a cylinder with a hemispherical bottom. The diameter is 6 cm and the height of the cylinder is 3 cm.

The bowl of glass 3 is an inverted cone. The diameter is 6 cm and the slant height is 6 cm.

1. Find the vertical height of the bowl of glass 3. Show your work.

**Pythagorean theorem:** radius = 3

$$6^2 = 3^2 + b^2 \quad b = \sqrt{27} = b = 3\sqrt{3}$$

$$b^2 = 6^2 - 3^2$$

$$b^2 = 36 - 9$$

$$\sqrt{b^2} = \sqrt{27}$$

$$3\sqrt{3} \text{ or } 5.2 \text{ cm.}$$

2. Calculate the volume of the bowl of each of these glasses. Show your work.

- a. Glass 1

$$\text{radius} = d \div 2 \quad 5 \div 2 = 2.5 = \text{radius} \quad 6 = \text{height}$$

$$2.5^2(6)\pi = 6.25 \cdot 6\pi = 37.5\pi \quad \boxed{117.75 \text{ cm}^3}$$

$$\frac{117.8}{37.5\pi} \text{ cm}^3$$

- b. Glass 2

$$\text{sphere} = \frac{4\pi r^3}{3} = \frac{4\pi 3^3}{3} = \frac{4\pi 27}{3} = \frac{108\pi}{3} = 36\pi \div 2 = 18\pi \quad 45\pi \text{ or } 141.37 \text{ cm}^3$$

$$\text{cylinder} = \pi r^2 h = \pi 3^2 \cdot 3 = \pi 9 \cdot 3 = 27\pi$$

$$\text{cylinder} + \text{hemisphere} = \text{glass 2}$$

$$27\pi + 18\pi = 45\pi \text{ or } \boxed{141.3 \text{ cm}^3}$$

because need to make it a hemisphere

- c. Glass 3

From problem 1 you get the height of it which is  $3\sqrt{3}$ . radius = 3

$$\text{Cone} = \frac{\pi 3^2 \cdot 3\sqrt{3}}{3} = \pi 3^2 \sqrt{3} = \pi 9\sqrt{3} = 5.588\pi$$

$$\approx 15.6\pi$$

$$\text{or } \boxed{48.9 \text{ cm}^3}$$

$$15.6\pi \text{ or } 48.97 \text{ cm}^3$$

3. Find the height of liquid in Glass 2 when it is half full. Show your calculations.

height of hemisphere = 3 3cm already filled

3.5 ✓ cm 1

$45\pi = \text{height of glass 2}$

$45\pi \div 2 = \text{mdpt} = 22.5\pi - \text{Liquid}$

$22.5\pi - 18\pi = 4.5\pi$  ✓: Bottom is full so only the sphere is remained

$4.5\pi = (3^2 \cdot h \pi) = \text{volume of cylinder}$  ✓

$$4.5\pi = 9h\pi$$

$$\frac{4.5}{9} = \frac{9h}{9}$$

$$h = .5$$
 ✓

.5 from cylinder plus hemisphere 3cm equals

3.5 cm

$$.5 + 3 = 3.5$$

3

Glasses

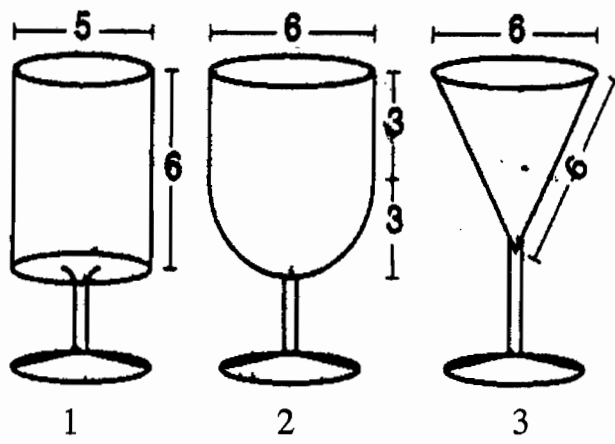
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The bowl of glass 1 is cylindrical. The diameter is 5 cm and the height is 6 cm.

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The bowl of glass 3 is an inverted cone. The diameter is 6 cm and the slant height is 6 cm.

1. Find the vertical height of the bowl of glass 3. Show your work.

$$3^2 + x^2 = 6^2$$

$$9 + x^2 = 36$$

$$x^2 = 27$$

$$x = \sqrt{27} = 3\sqrt{3}$$

3√3 cm ✓

2. Calculate the volume of the bowl of each of these glasses. Show your work.

a. Glass 1

$$\pi \cdot 2.5^2 \cdot 6$$

$$\pi \cdot 6.25 \cdot 6$$

37.5π cm<sup>3</sup> ✓

b. Glass 2

$$4\pi \cdot 3^3 = 27\pi$$

$$\frac{36\pi \cdot \frac{1}{2}}{3} = 6\pi$$

$$27\pi - 6\pi = 21\pi$$

45π cm<sup>3</sup> ✓

c. Glass 3

$$\pi \cdot 3^2 \cdot 3 = 27\pi$$

$$\frac{\pi \cdot 9 \cdot 3\sqrt{3}}{3} = 9\pi\sqrt{3}$$

π 9√3 cm<sup>3</sup> ✓

3. Find the height of liquid in Glass 2 when it is half full. Show your calculations.

$3\frac{1}{2}$  ✓ cm 1

$22.5\pi$

4.5π of the cylinder

$\frac{4.5}{27} \times \frac{1}{6} \times 3 = \frac{1}{2}$  cm

(2)

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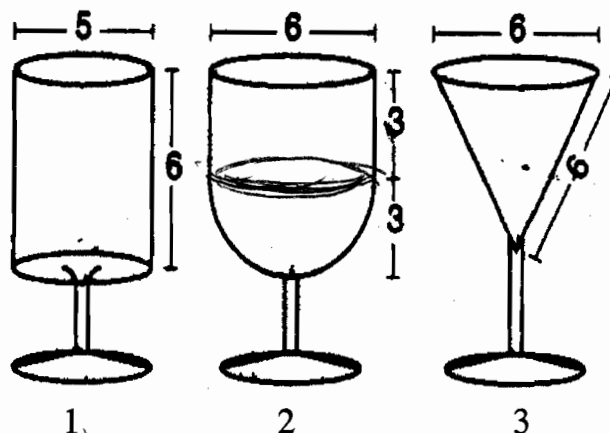
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1. Find the vertical height of the bowl of glass 3. Show your work.

$$\frac{6}{2} = 3$$

$$3^2 + z^2 = 36$$

$$9 + z^2 = 36$$

$$z^2 = 27$$

$$z = 5.196$$

$$\underline{5.196 \text{ cm}}$$

2. Calculate the volume of the bowl of each of these glasses. Show your work.

a. Glass 1

$$(2.5)^2 (6) (\pi) = 117.81$$

$$\underline{117.81 \text{ cm}^3}$$

b. Glass 2

$$(3)^2 (3) (\pi) + \frac{4\pi (3)^3}{3 \cdot 2} = 84.823 + 56.55 = 141.372$$

$$\underline{141.37 \text{ cm}^3}$$

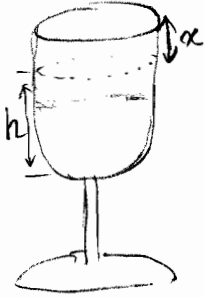
c. Glass 3

$$\frac{\pi (3)^2 (5.196)}{3} = 3\pi (5.196) = 48.97114628$$

$$\underline{48.97 \text{ cm}^3}$$

3. Find the height of liquid in Glass 2 when it is half full. Show your calculations.

3.5 ✓ cm |



$$\frac{141.37}{2} = 70.685$$

$$9\pi(x) = 70.685$$

$$28.274x = 70.685$$

$$x = 2.5$$

$$h = 6 - 2.5 = 3.5$$

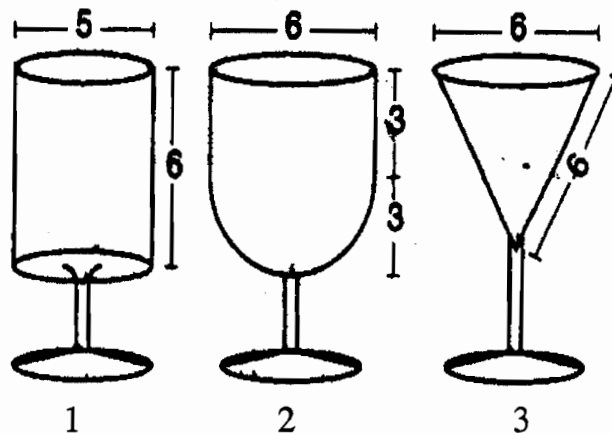
3

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$$3^2 + b^2 = 6^2$$

$$9 + b^2 = 36$$

$$b^2 = 27$$

$$b = 3\sqrt{3}$$

3√3 ✓ cm.

2. Calculate the volume of the bowl of each of these glasses. Show your work.

a. Glass 1

$$\pi(2.5^2)6$$

$$\pi(6.25)6$$

$$37.5\pi \quad 37.5(3.14) \quad 117.75$$

117.75 ✓ cm<sup>3</sup>

b. Glass 2

$$\pi(3^2)3$$

$$\pi(9)3$$

$$27\pi$$

$$\frac{1}{2} \left( \frac{\pi(3^2)}{3} \right)$$

$$\frac{2\pi(27)}{3}$$

$$18\pi$$

$$27\pi + 18\pi$$

$$45\pi$$

$$45(3.14)$$

$$141.3$$

141.3 ✓ cm<sup>3</sup>

c. Glass 3

$$\frac{\pi(3^2)(3\sqrt{3})}{3}$$

$$\frac{\pi(3^3)\sqrt{3}}{3}$$

$$\frac{\pi(3^2)\sqrt{3}}{3}$$

$$9\sqrt{3}\pi$$

$$9\sqrt{3}(3.14)$$

$$28.26\sqrt{3}$$

28.26√3 ✓ cm<sup>3</sup>

3. Find the height of liquid in Glass 2 when it is half full. Show your calculations.

$$\underline{3\frac{1}{2}} \checkmark \text{ cm } |$$

$$18\pi = \text{volume of hemisphere}$$

$$22.5\pi = \text{half of total volume}$$

$$27\pi = \text{volume of cylinder}$$

$$3 = \text{height of cylinder}$$

$$\begin{array}{r} 22.5\pi - 18\pi \\ \hline 4.5\pi \end{array} \checkmark$$

$$\frac{4.5\pi}{27\pi} \quad \frac{9\pi}{54\pi} \quad \frac{1}{6}$$

$$\frac{1}{6} \cdot 3 = \frac{3}{6} = \frac{1}{2} \checkmark$$

$$3 + \frac{1}{2} = 3\frac{1}{2}$$

3



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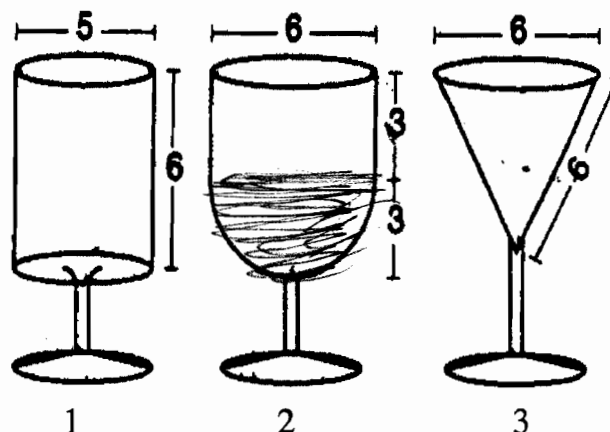
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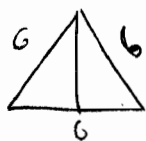


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1. Find the vertical height of the bowl of glass 3. Show your work.



$$\begin{aligned} a^2 + b^2 &= c^2 \\ a^2 + 9 &= 36 \\ a^2 &= 27 \\ a &= \sqrt{27} \approx 5.196 \end{aligned}$$

≈ 5.2 cm ✓

2. Calculate the volume of the bowl of each of these glasses. Show your work.

a. Glass 1

$$\pi r^2 h = \pi (2.5)^2 (6) = (6.25)(6)\pi = 37.5\pi$$

$$(\approx 117.75)$$

$$\begin{array}{r} 37.5 \\ \times 3.14 \\ \hline 1500 \\ 375 \\ \hline 117.75 \end{array}$$

≈ 117.75 cm<sup>3</sup> ✓

b. Glass 2

$$\pi r^2 h = \pi (3)^2 (3) = 27\pi$$

$$\frac{4\pi r^3}{3} = \frac{4(3)^3\pi}{3} = 36\pi \text{ hemisphere } \rightarrow 18\pi$$

$$27\pi + 18\pi = 45\pi (\approx 141.3)$$

$$\begin{array}{r} 45 \\ \times 3.14 \\ \hline 1570 \\ 1266 \\ \hline 141.30 \end{array}$$

≈ 141.3 cm<sup>3</sup> ✓

c. Glass 3

$$\frac{\pi r^2 h}{3} = \frac{\pi (3)^2 (5.2)}{3} = 15.6\pi$$

$$(\approx 48.984)$$

$$\begin{array}{r} 15.6 \\ \times 3.14 \\ \hline 624 \\ 156 \\ \hline 48.984 \end{array}$$

≈ 48.98 cm<sup>3</sup> ✓

3. Find the height of liquid in Glass 2 when it is half full. Show your calculations.

Vol. of glass 2:  $45\pi$      $\frac{45\pi}{2} = 22.5\pi$

$3\frac{1}{2}$  ✓ cm |

$22.5\pi - 18\pi = 4.5\pi$  ✓

↑  
vol. of  
hemisphere

$\frac{27\pi}{3} = \frac{9\pi}{1} = 9\pi$  of liquid per cm ✓

↑  
vol. of  
cylinder

$9\pi - 4.5\pi = 4.5\pi$

( $4.5\pi$  is half of  $9\pi$ ,  
so

$3 + \frac{1}{2} = 3\frac{1}{2}$ ) ✓

3

