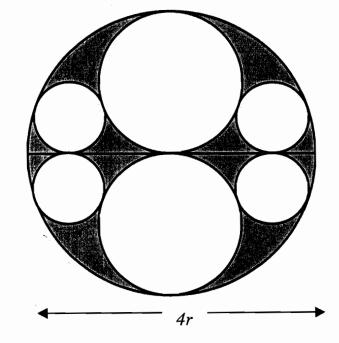
During the Edo period (1603-1867) of Japanese history, geometrical puzzles were hung in the holy temples as offerings to the gods and as challenges to worshippers.

This is one such problem.

Inside a large circle with radius 2r, two circles of radius r are drawn.

Four smaller circles, of radius p, are drawn to touch the large circle and the circles of radius r.



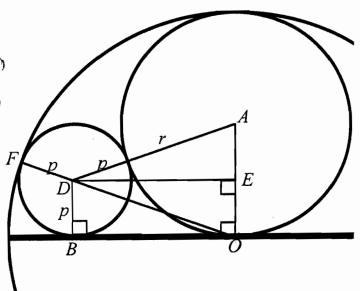
The following questions will help you to find the relationship between r and p

1. In the right triangle DOB, explain why the length of OD is 2r - p

FO is radius of large circle (ar)

FD is radius of small circle (P)

OD = FO - FD = 2r -P



3. In the right triangle ADE, explain why the length of AE is r - p.

4. Use the Pythagorean theorem in triangle ADE to find an expression for ED<sup>2</sup>.

$$DE^{3} = AD^{3} - AB^{2} = (r+p)^{2} - (r-p)^{2} = v^{2} + 2rp+p^{2} - (r^{2} - 2rp+p^{2})$$

$$fp^{2} = 4rp$$

5. Use your results from questions 2 and 4, and the fact that OB = ED to show that r = 2p

$$\overline{OB}^2 = \overline{ED}^2 \qquad 4rp = 4r^2 \quad 4rp \qquad 8rp = 4r^2 \quad 2rp = r^2 \quad 2p = r$$

6. Show that the shaded area of the diagram has area  $\pi r^2$ .

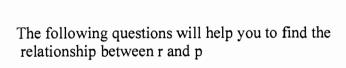
Shaded Area = 
$$\pi(2r)^2 - 2\pi(c)^2 - 4\pi(4r)^2$$
  
 $-4\pi r^2 - 2\pi r^2 - \pi r^2$   
 $=\pi r^2$ 

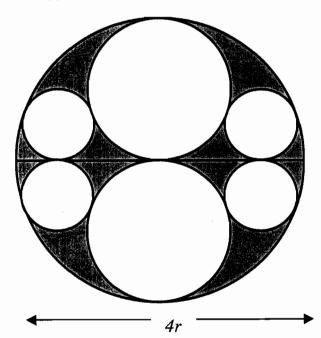
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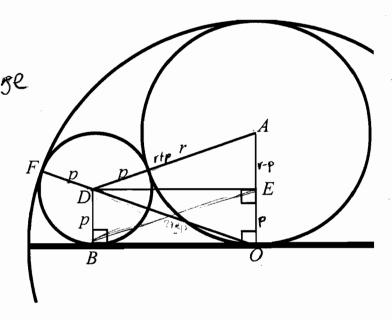


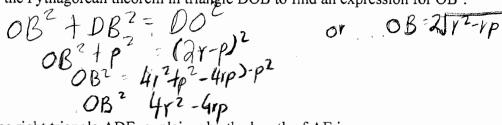


1. In the right triangle DOB, explain why the length of OD is 2r - pOF 13 the radius of the large

of the smallest. The length of OD must be OF-FD

=2r-p.





3. In the right triangle ADE, explain why the length of AE is r - p.

4. Use the Pythagorean theorem in triangle ADE to find an expression for ED<sup>2</sup>.

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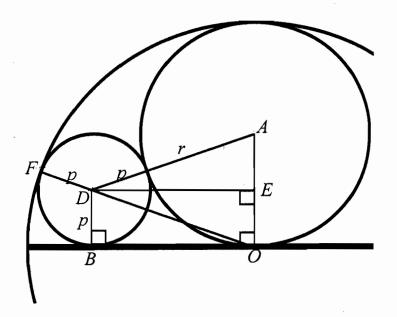
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4r

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1. In the right triangle DOB,
explain why the length of OD is 2r - p

$$\frac{OO = OF - FD}{OO = 2r - P}$$



$$DB^{2} + OB^{2} = DO^{2}$$

$$p^{2} + OB^{2} = (2r-p)^{2}$$

$$OB^{2} = (2r-p)(2r-p) - p^{2}$$

$$OB^{2} = 4r^{2} - 2pr - 2pr - 2$$

$$OB^{2} = 4r^{2} - 2pr - 2pr - 2$$

3. In the right triangle ADE, explain why the length of AE is r - p.

4. Use the Pythagorean theorem in triangle ADE to find an expression for ED<sup>2</sup>.

$$AD = P + r \quad AE = r - p \qquad (r - p)^{2} + Ep^{2} = (p + r)^{2}$$

$$ED^{2} = p^{2} + 2pr + r^{2} - (r^{2} - 2pr + p^{2})$$

$$ED^{2} = 4pr$$

5. Use your results from questions 2 and 4, and the fact that OB = ED to show that r = 2p  $\frac{4r^2 - 4pr}{4r^2} = 4pr \qquad 4r^2 = 8pr \qquad r = 2p$ 

6. Show that the shaded area of the diagram has area  $\pi r^2$ .

Big circle:  $4 r^2 \pi$ 2 medium circle:  $2\pi r^2$ 4 small circle:  $4p^2\pi$   $4p^2\pi$ 

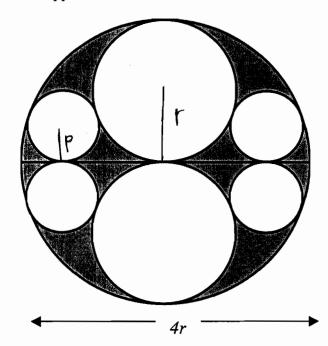
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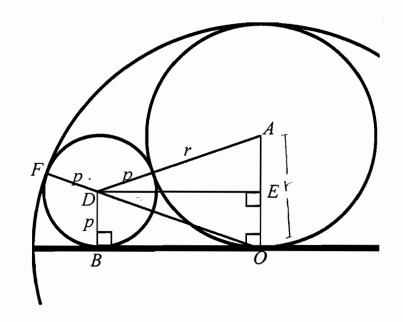
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The following questions will help you to find the relationship between r and p



1. In the right triangle DOB, explain why the length of OD is 2r - p

od is 2r-placeause the radius of the big circle is 2r, and the radius of small is p. OD+p=2r. (all radii of a 0 ?) To get od, od=2r-p



2. Use the Pythagorean theorem in triangle DOB to find an expression for OB<sup>2</sup>.

OB 
$$^{2}$$
 +  $^{2}$  =  $(21 - ^{2})^{2}$ 

OB  $^{2}$  =  $41^{2} - 41^{2}$  +  $^{2}$  -  $^{2}$ 

3. In the right triangle ADE, explain why the length of AE is r - p.

4. Use the Pythagorean theorem in triangle ADE to find an expression for ED<sup>2</sup>.

$$ED^2 + (1-p)^2 = (p+r)^2$$
;  $ED^2 + r^2 - 2pr + p^2 = p^2 + 2pr + r^2$ .

$$fD^2 = p^2 + 2pr + r^2 - r^2 + 2pr - p^2$$
;  $fD^2 = 4pr$   
 $(r-p)(r-p)$   $(p+r)(p+r)$ 

5. Use your results from questions 2 and 4, and the fact that OB = ED to show that r = 2p

6. Show that the shaded area of the diagram has area  $\pi r^2$ .

area of and =  $\pi radius^2$ ; by anch =  $\pi(2r)^2 = \pi 4r^2$ . medium

anch =  $\pi r^2$ . Since r = 2p, 2 small arch 's area = 1 mf Jium.

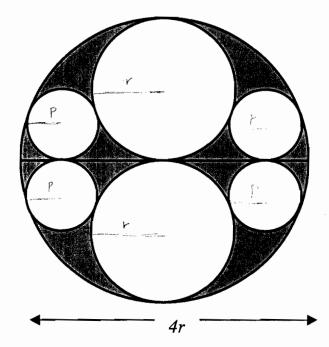
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od is 2r-p because od FD= 2r

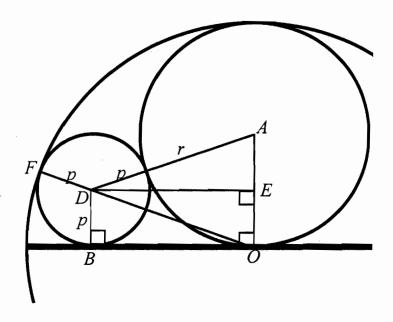
since that lines draws the radius of

the largest circle. FD is the radius

of the smallest circle so OF-FD= od and

by substituting the radii values you get

2r-p.



$$(2r-p)(2r-p)$$
  $(2r-p)^2 - (p)^2 = 0B^2$   
 $4r^2 - 4pr + p^2 - p^2 = 0B^2$   
 $4r(r-p) = 0B^2$ 

3. In the right triangle ADE, explain why the length of AE is r - p.

4. Use the Pythagorean theorem in triangle ADE to find an expression for ED<sup>2</sup>.

$$\frac{(r+p)^{2}-(r-p)^{2}=ED^{2}}{ED^{2}=4pr}$$

$$\frac{(r+p)(r+p)}{(r+p)}\frac{(-r+p)(-r+p)}{(-r+p)}$$

$$\frac{r^{2}+pr^{2}+pr^{2}+pr^{2}}{r^{2}+2pr+p^{2}}$$

$$\frac{r^{2}-pr-pr+p^{2}}{r^{2}-2pr+p^{2}}$$

5. Use your results from questions 2 and 4, and the fact that OB = ED to show that r = 2p

$$\overline{OB} \cong \overline{ED} \text{ so } 4r^2 - 4pr = 4tpr$$

$$4r^2 = 8pr \text{ so } r = 2p$$

$$4r \overline{4r}$$

6. Show that the shaded area of the diagram has area  $\pi r^2$ .

Area of largest circle =  $4\pi r^2$ Area of 2 circles w/radius  $r = 2\pi r^2$ Area of 4 circles w/radius  $\frac{r}{2} = \pi r^2$ Area of 4 circles w/radius  $\frac{r}{2} = \pi r^2$