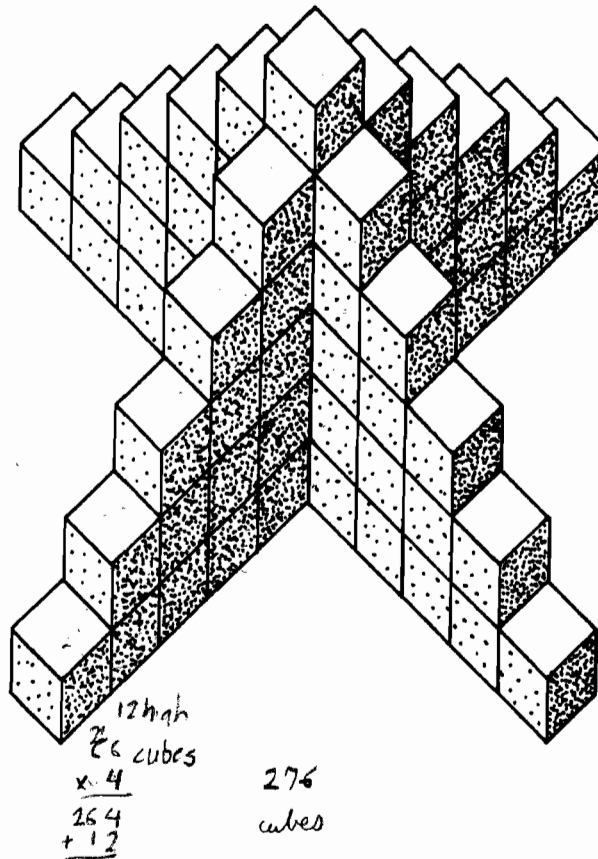


$$\begin{array}{r} \times \\ 60 \\ + 6 \\ \hline 66 \end{array}$$



1. How many cubes are needed to build this tower?
Show your calculations

66 cubes

2. How many cubes are needed to build a tower like this, but 12 cubes high?
Explain how you figure out your answer.

276 cubes

for this problem only 1 cube is alone on top with a single row of cubes going down center. However 11 rows of cubes aren't attached to middle row. From the 5 rows already shown add another row with 1 extra up to 11 rows to 66 cubes multiply by 4 to get 264 cubes and add the 12 middle row to get 276 cubes

Skeleton Tower (continued)

3. How would you calculate the number of cubes needed for a tower n cubes high?

no of cubes in each wing is $1+2+3+4+\dots+(n-1)$ which is $\frac{n(n-1)}{2}$

*There are 4 wings so the number of cubes is $\frac{4n(n-1)}{2}$

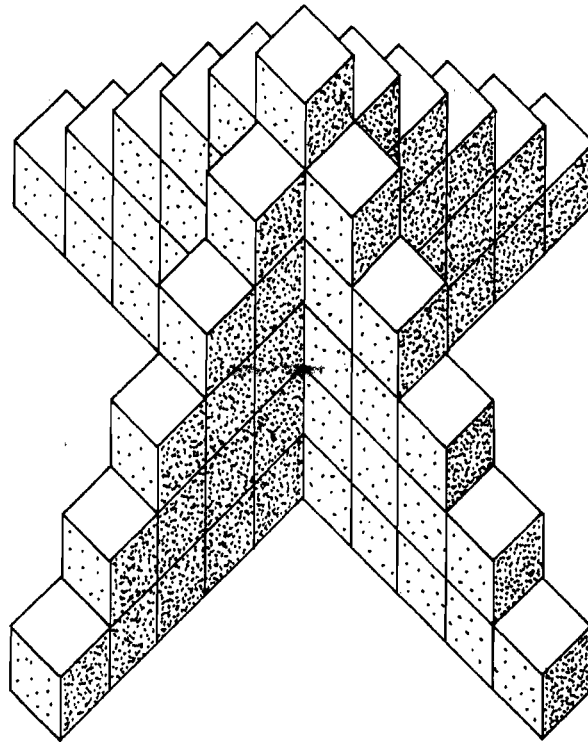
This does not include the number of cubes down the centre

so the complete formula for the number of cubes is

$$\frac{4n(n-1)}{2} + n = 2n(n-1) + n = 2n^2 - 2n + n = 2n^2 - n$$

check $n=5$ $2 \cdot 5^2 - 5 = 72 - 5 = 67 \checkmark$

$n=12$ $2 \cdot 12^2 - 12 = 288 - 12 = 276 \checkmark$



1. How many cubes are needed to build this tower?
Show your calculations

66

each side w/o center post has height $(1+2+3+4+5) = 15$
 4 sides = 60
 + 6 cubes in center = 66

2. How many cubes are needed to build a tower like this, but 12 cubes high?
Explain how you figure out your answer.

276

$12 + 4(1+2+\dots+11)$ $12 + 4((12 \cdot 5) + 6) = 12 + 4(66) = 12 + 264 = 276$

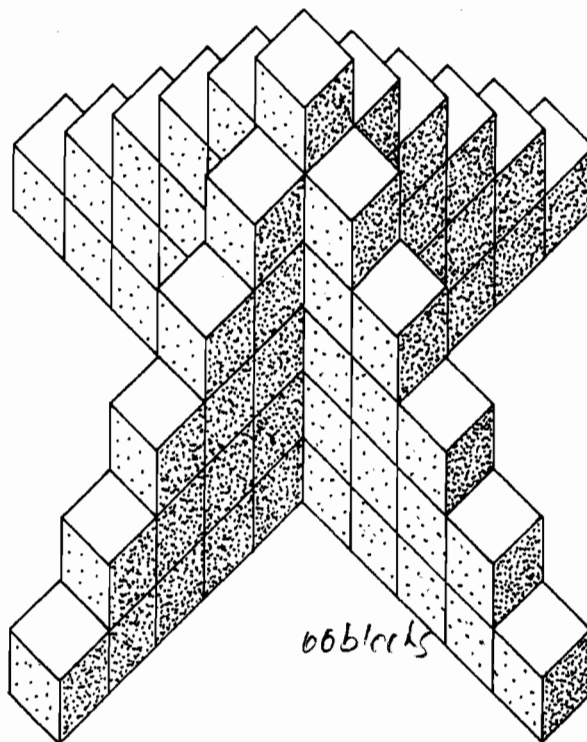
(I found the formula first)

Skeleton Tower (continued)

3. How would you calculate the number of cubes needed for a tower n cubes high?

$$n + 4(1+2+\dots+(n-1))$$

4 sides w/o center would always be $1+2+3+4+\dots$ until the number just before $n:(n-1)$, the center post is the highest, so the height n of the tower determines how tall the center post is



1. How many cubes are needed to build this tower?
Show your calculations

66 cubes

$$15 \times 4 + 5 + 1 = 66$$

2. How many cubes are needed to build a tower like this, but 12 cubes high?
Explain how you figure out your answer.

276 cubes

$x = \text{height of tower}$ Formula each wing # of blocks = $\frac{(x-1)x}{2}$
 Total blocks 4 wings = $4 \times \frac{(x-1)x}{2} = 2x(x-1)$
 center tower blocks: x

$$\text{Total \# of blocks of entire tower} = 2x(x-1) + x =$$

$$2x^2 - 2x + x =$$

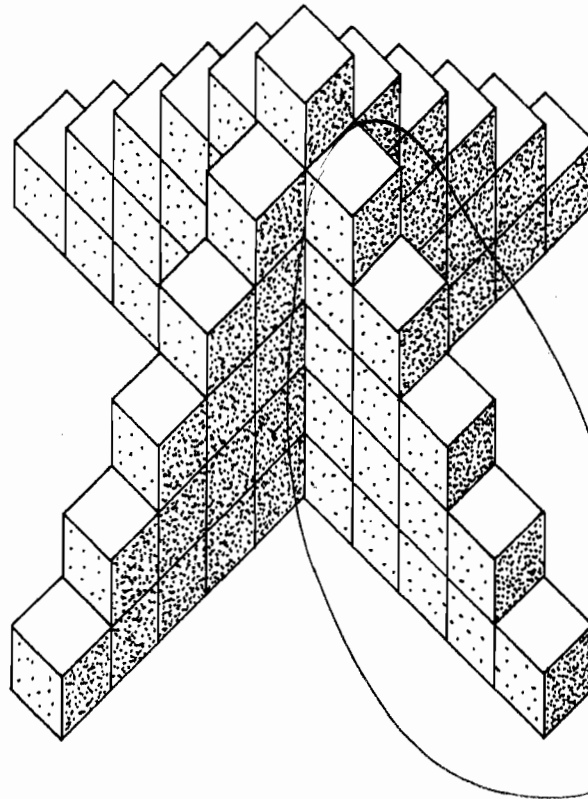
$$2x^2 - x$$

$$2(12)^2 - 12 = 288 - 12 = 276$$

Skeleton Tower (continued)

3. How would you calculate the number of cubes needed for a tower n cubes high?

$$2 \cdot n^2 - n$$



1. How many cubes are needed to build this tower?

Show your calculations

$$\begin{array}{r} 15 \\ \times 4 \\ \hline 60 \end{array}$$

$$\begin{array}{r} 60 \\ + 6 \\ \hline 66 \end{array}$$

66 cubes

2. How many cubes are needed to build a tower like this, but 12 cubes high?

Explain how you figure out your answer.

276 cubes

$$1+2+3+4+5+6+7+8+9+10+11=66$$

$$(66)(4) = 264$$

$$264 + 12 = 276$$

Skeleton Tower (continued)

3. How would you calculate the number of cubes needed for a tower n cubes high?

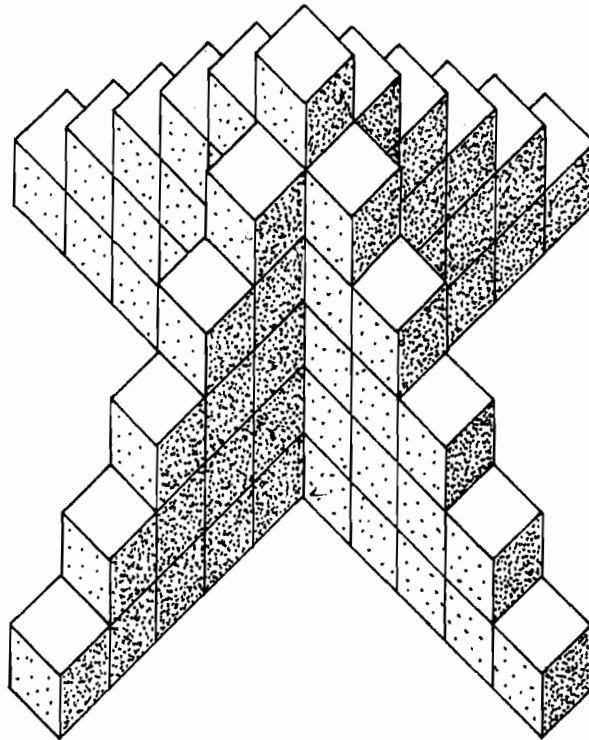
$$1 + 2 + 3 + \dots + (n-1) = \frac{n(n-1)}{2}$$

$$4 \left(\frac{n(n-1)}{2} \right) + n$$

$$4 \left(\frac{n^2 - n}{2} \right) + n$$

$$2n^2 - 2n + n$$

$$\boxed{2n^2 - n}$$



1. How many cubes are needed to build this tower?
Show your calculations

66 cubes

$$4(5+4+3+2+1) + 6$$

\uparrow \uparrow \uparrow
 # of sides sides middle column

2. How many cubes are needed to build a tower like this, but 12 cubes high?
Explain how you figure out your answer.

270 cubes

I used the formula $4(11+10+9+8+7+6+5+4+3+2+1) + 12$

$$= 4(66) + 6 = 264 + 6 = 270$$

Skeleton Tower (continued)

3. How would you calculate the number of cubes needed for a tower n cubes high?

I would use the formula $4 \left(\frac{n(n-1)}{2} \right) + n$

sides of tower

of cubes
center column
height

of cubes per

side $(1+2+3+4+\dots+(n-1))$